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# **SMAP L3\_SM\_A/P High Resolution Soil Moisture Algorithm Status and Issues**

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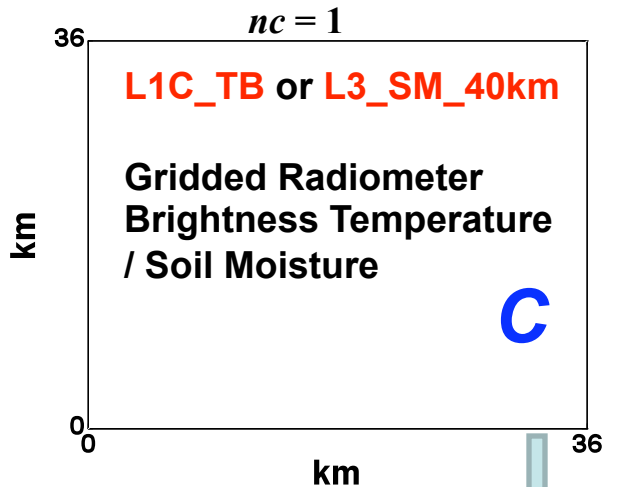
SMAP Algorithms and Calibration/Validation Workshop

June 9-11, 2009

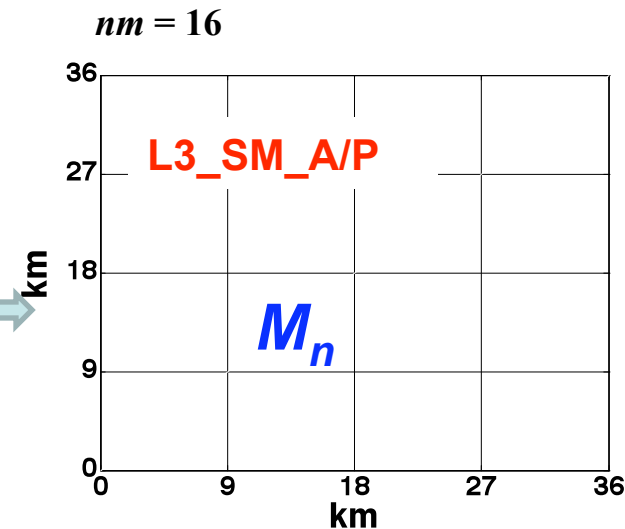
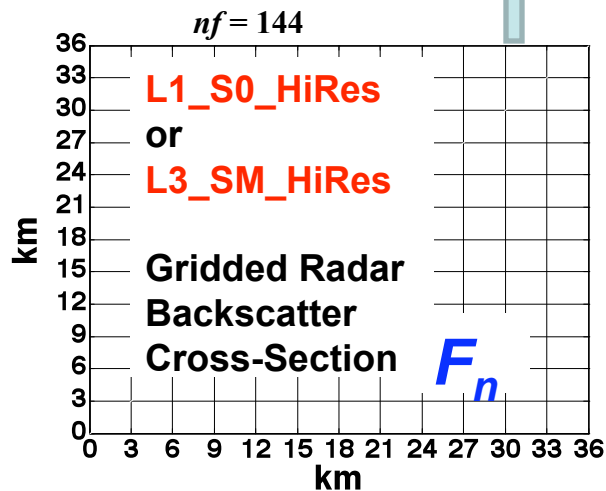
Oxnard, CA



# Grid Definitions



Merge  
Algorithm



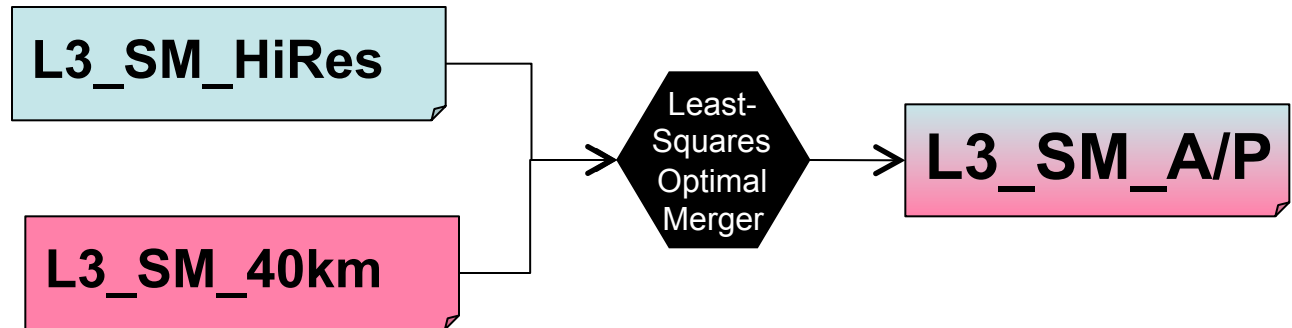
C = Coarse (~36 km Radiometer)  
M = Medium (~9 km Merged Product)  
F = Fine (~3 km Radar)



# Approaches

## Approach 1:

Begins with L3  
Retrieved Soil  
Moisture Products

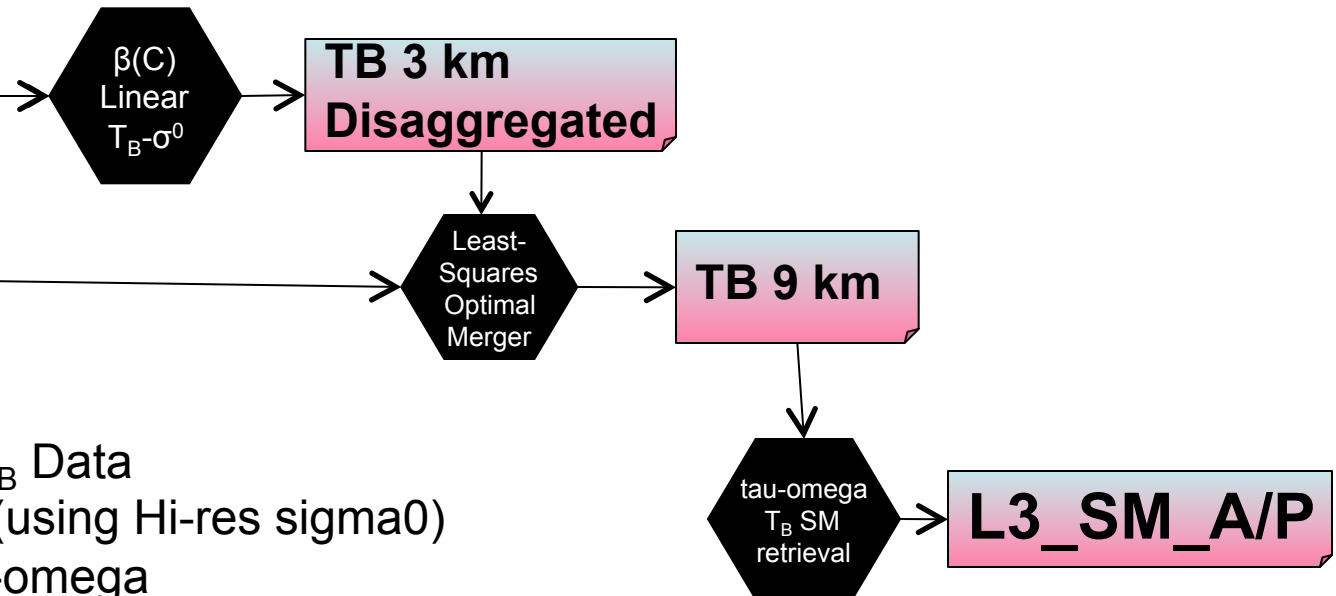


**L1C\_S0\_HiRes**

**L1C\_TB**

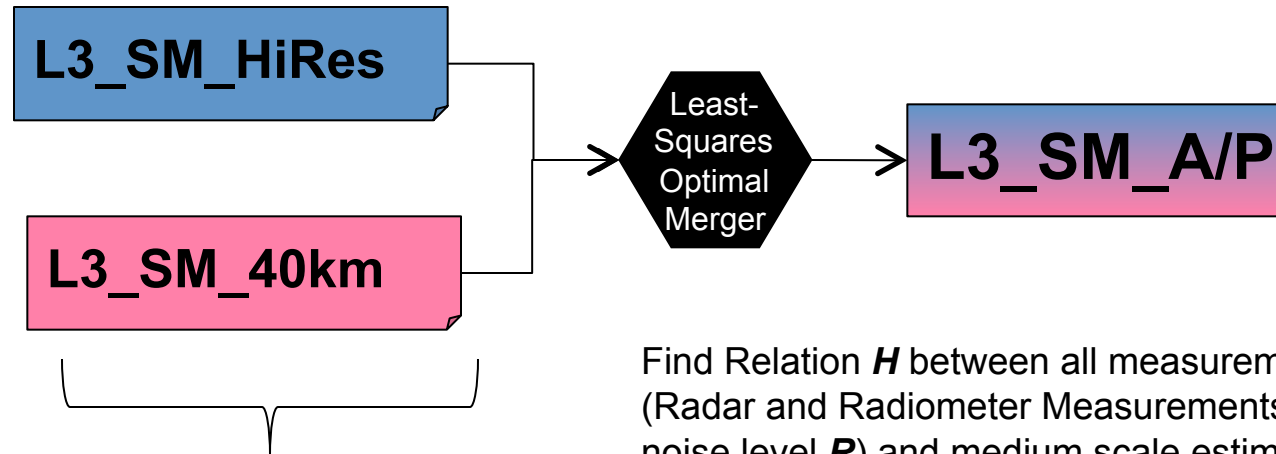
## Approach 2:

- Begins with L1C  $T_B$  Data
- Disaggregates  $T_B$  (using Hi-res sigma0)
- Retrieval With tau-omega





# Approach 1



Collect  
multiple  
scale data  
into an  
observation  
vector:

$$Z = \begin{bmatrix} \theta_C \\ \theta_{F1} \\ \theta_{F.2} \\ \vdots \\ \theta_{F.nf} \end{bmatrix}$$

Find Relation  $H$  between all measurements  
(Radar and Radiometer Measurements  $Z$  with RMSE  
noise level  $R$ ) and medium scale estimates of soil  
moisture.

Pose Least-Squares Estimation Problem:

$$E = [Z - H \cdot \theta(M_n)]^T R^{-1} [Z - H \cdot \theta(M_n)]$$

Solution: 
$$\theta(M_n) = \left[ (H^T R^{-1} H)^{-1} H^T R^{-1} \right] \cdot Z$$

## Advantages:

1. Least-Squares Beats Down Error (Oversampling)
2. Provides Confidence Limits on Estimates

## Disadvantages:

1. Relies on L3 Retrieved SM Products
2. Needs *Unbiased* L3 Products

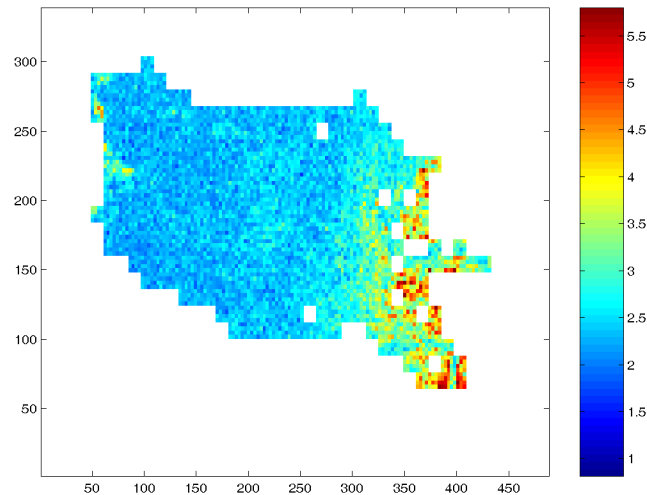


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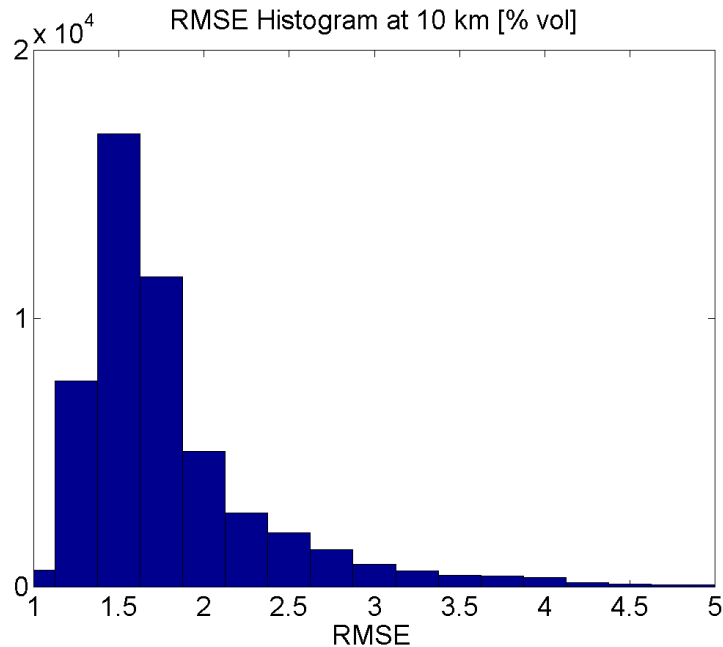
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# Approach 1

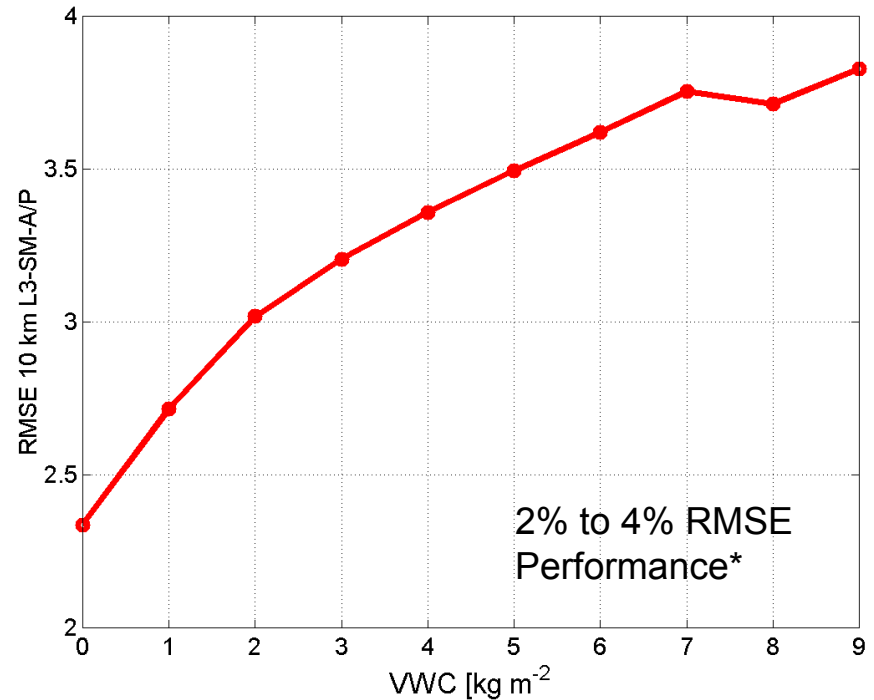
RMSE Field at 10 km [% vol]



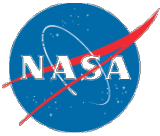
RMSE Histogram at 10 km [% vol]



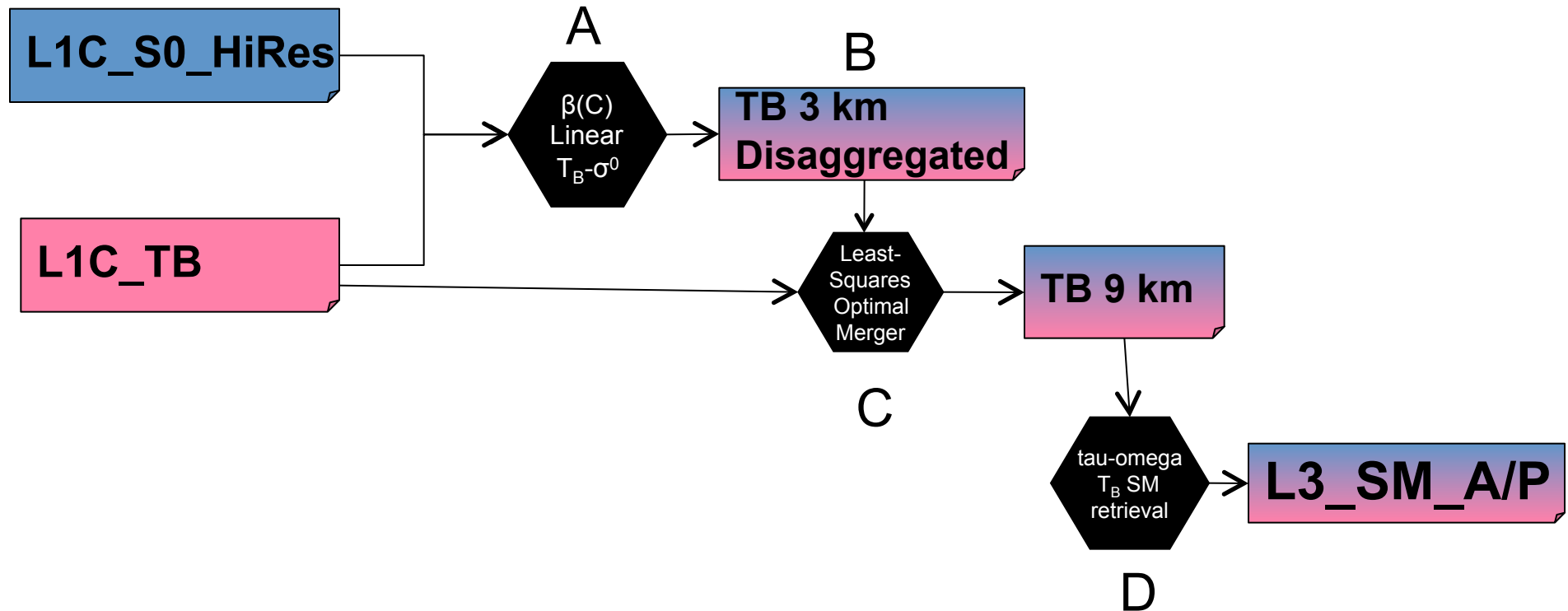
2 X VWC OSSE



Approach 1 Performance Over  
Red-River OSSE (1 Month) With  
Noise Added



# Approach 2



## Advantages:

1. Uses L1C\_TB Instrument Data directly
2. Removes Bias through  $T_B$  Aggregation Rule
3. Uses Least-Squares to Beats Down Error
4. Uses same tau-omega Retrieval Code as L3\_SM\_40km
5. Can Use PALS  $T_B$  and  $\sigma^0$  Data to Test

## Disadvantages:

1. Assumes Linear Relation Between  $T_B$  and  $\sigma^0$  (dB)
2. Linear Coefficient is Vegetation-Dependent and assumed to be spatially homogeneous within 36 km



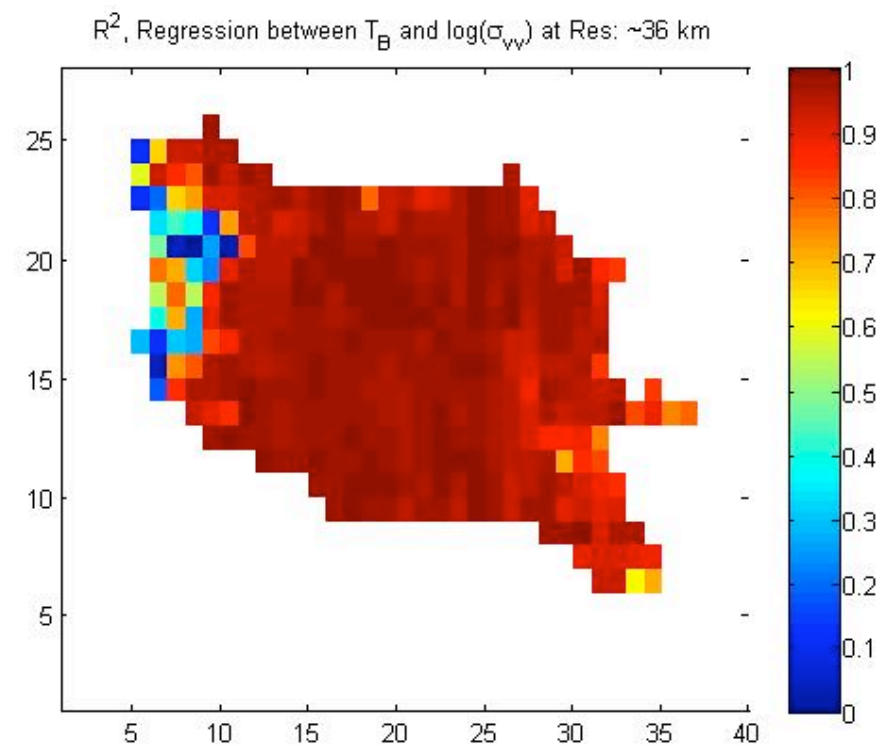
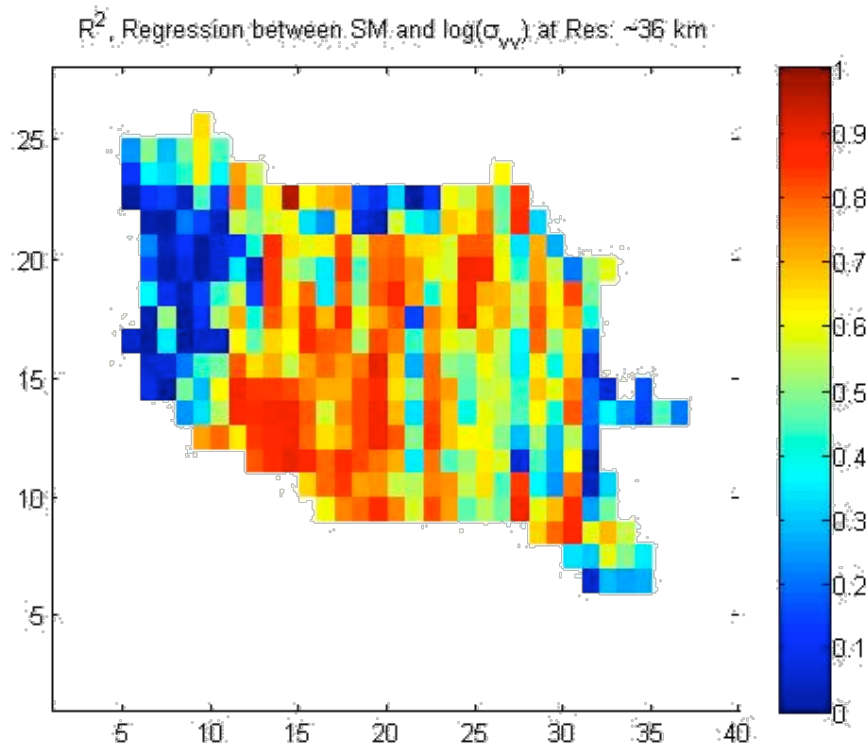
# Linear Relationship between $T_B$ and $\Sigma_0$

## Part (A) of Approach 2

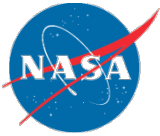
At the radiometer scale- $C$  use time-series of brightness temperature and aggregated radar backscatter ( $\log_{10}$ ) to develop linear model.

$$SM(C, t) = \alpha(C) + \beta(C) \log_{10} \left( \frac{1}{nf} \sum_{i=1}^{nf} \sigma_{vv}(F_i, t) \right)$$

$$T_B(C, t) = \alpha(C) + \beta(C) \log_{10} \left( \frac{1}{nf} \sum_{i=1}^{nf} \sigma_{vv}(F_i, t) \right)$$



Better  $R^2$  values are observed for ( $T_B$  and  $\text{Mean}[\log(\sigma_{vv})]$ ) as compared to ( $SM$  and  $\text{Mean}[\log(\sigma_{vv})]$ )



# Disaggregation of $T_B$ using Fine Scale Sigma0

## Part (B) of Approach 2

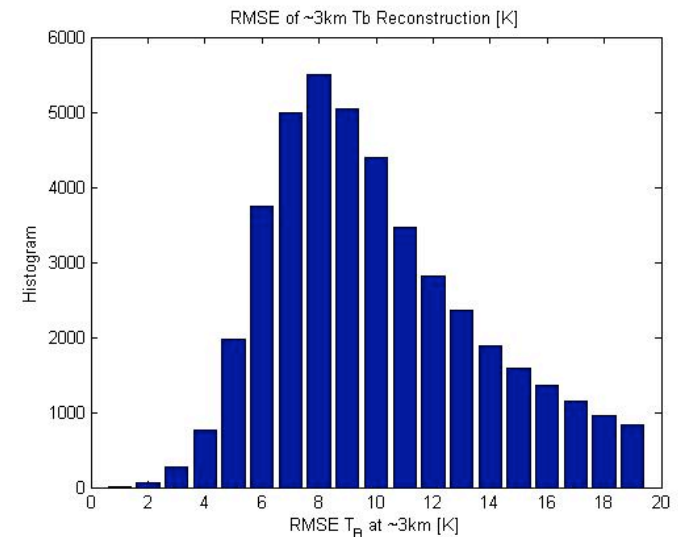
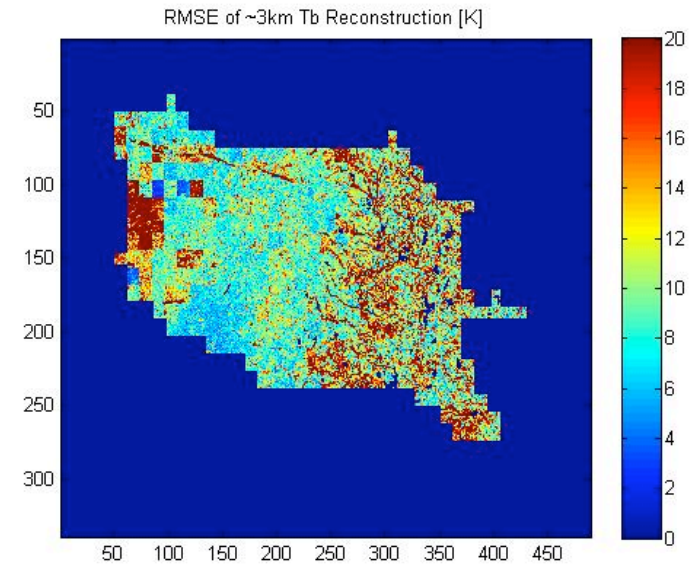
The fine-scale brightness temperature is taken to be the coarse-scale brightness temperature adjusted by radar-based spatial anomalies (symbolized by  $\delta$ ) as in

$$T_B(F_i, t) = T_B(C_i, t) + \beta(C) \cdot \delta \log_{10}(\sigma_{vv}(F_i, t))$$

Parameter  $\beta(C)$  is assumed to be applicable at the finer scales, i.e. heterogeneity at larger scales and homogeneous within coarse scale

Bias is removed from the reconstruction by requiring that

$$T_B(C, t) = (1/nf) \left( \sum_{i=1}^{nf} \log_{10}(T_B(F_i, t)) \right)$$



RMSE of 3km Reconstructed  $T_B$  in the SMAP OSSE.  
Anticipated radar and radiometer noise levels are added.

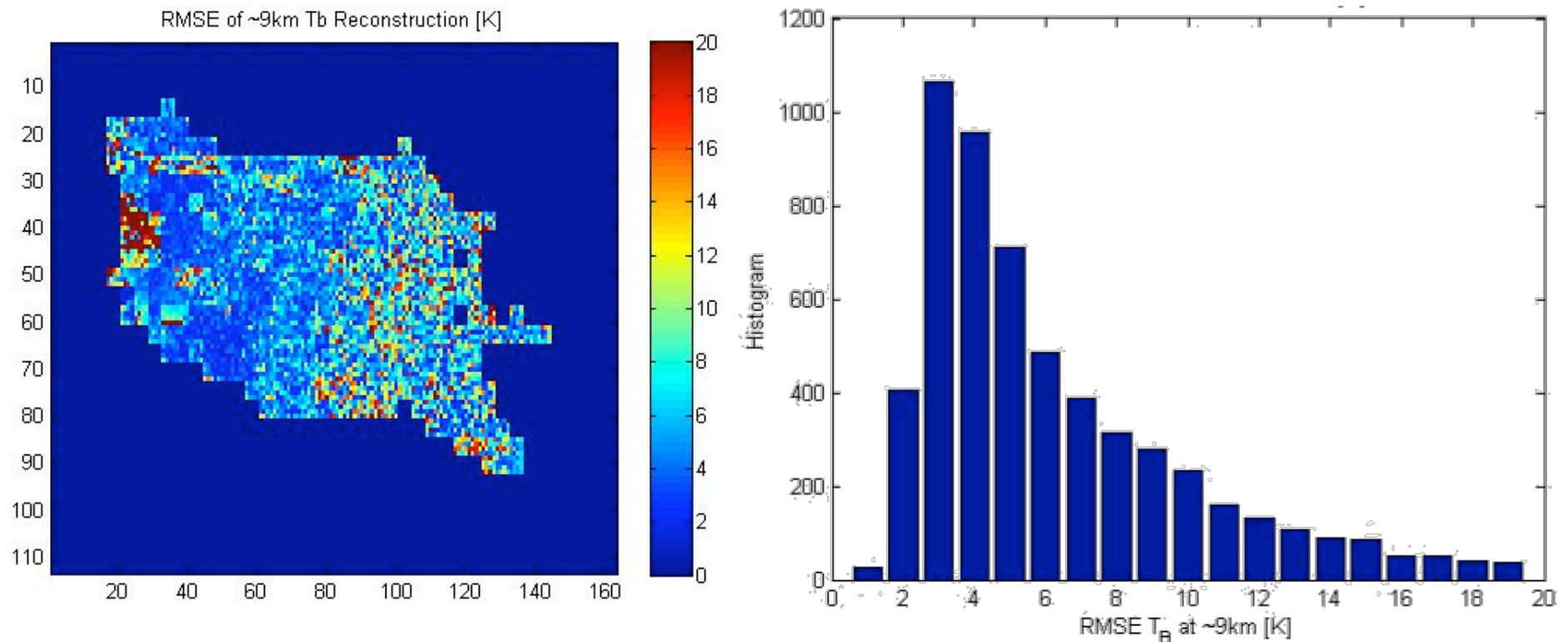




## Optimal Merger of Coarse Scale $T_B$ with Fine Scale $T_B$

### Part (C) of Approach 2

Coarse Scale  $T_B$  (~36 km) blended with fine scale  $T_B$  (~3 km) using optimal merger to obtain medium resolution  $T_B$  (~9 km)



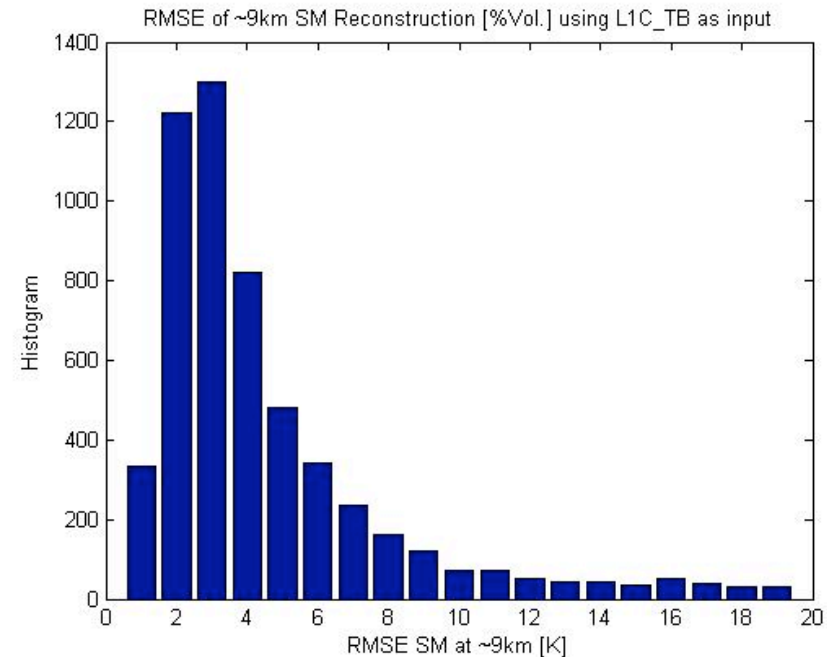
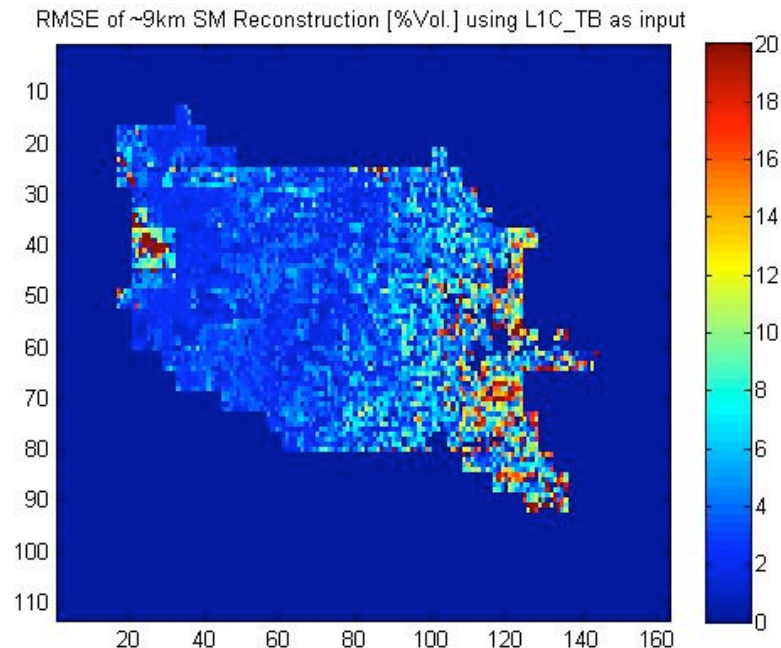
RMSE of 9km Reconstructed  $T_B$  in the OSSE.  
Anticipated radar and radiometer noise levels are added.



## Soil Moisture Performance at Scale of L3\_SM\_A/P

### Part (D) of Approach 2

The radiometer retrieval algorithms (see L3\_40km\_SM) are now applied to retrieve soil moisture. Required ancillary data are provided at 9 km.



RMSE of 9km Reconstructed soil moisture in the OSSE using Single-Channel Radiometer Algorithm. Anticipated radar and radiometer noise levels are added. The errors are largest where there is significant vegetation (East) or where  $\beta$  could not be estimated well due to persistent soil dryness (West).



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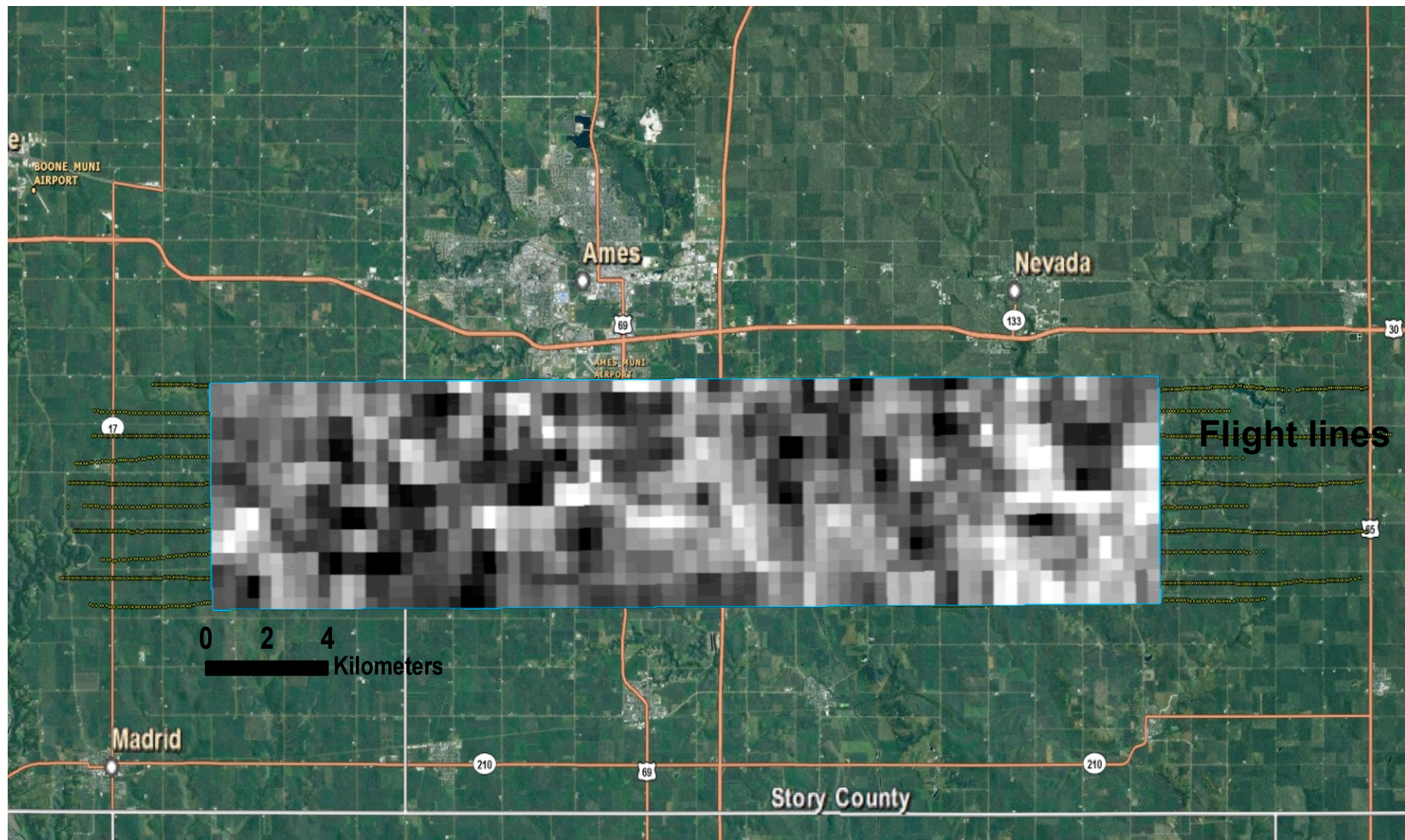
# Application of Approach 2 to Airborne Passive/Active L-/S-band (PALS) microwave data from SMEX02



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# Gridding of PALS Flight lines Data



TB data gridded at 4 km, and Sigma0 gridded at 0.4 km

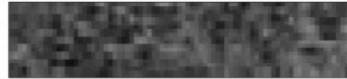




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# Evaluation of Linear Relationship Between $T_B$ and Sigma0 for PALS Data

$T_B$  (h-pol)    Res: 4 km    June 25, 2002    Res: 0.4 km    Sigma0 (vv)



June 27, 2002



July 02, 2002



July 05, 2002



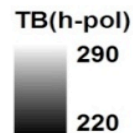
July 06, 2002



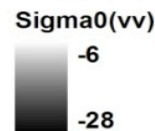
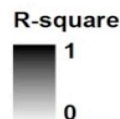
June 07, 2002



June 08, 2002



$R^2$

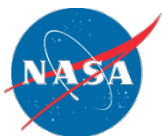


## PALS Explained Variance

7-days of SMEX02 PALS  $T_B$  and  $\sigma^0$

$T_B$  aggregated to form the same  
scale differences as with SMAP  
( $T_B \sim 4$  km and  $\sigma \sim 0.4$  km)

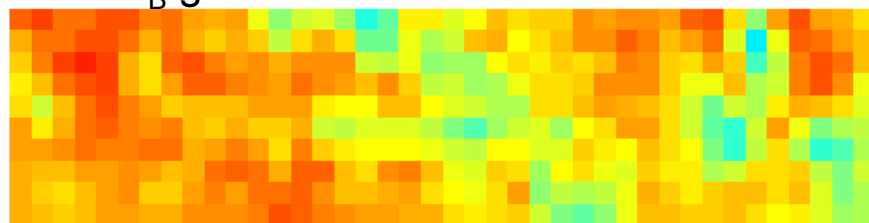
For 7-days the  $R^2$  field has  
Median value of 0.75  
(Max value of 0.91)  
(Min value of 0.44)



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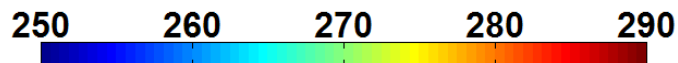
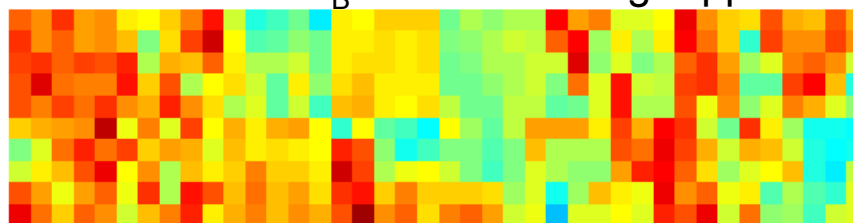
# Comparison of Reconstructed $T_B$ at 0.8 km with Gridded PALS data

PALS  $T_B$  gridded at 0.8 km

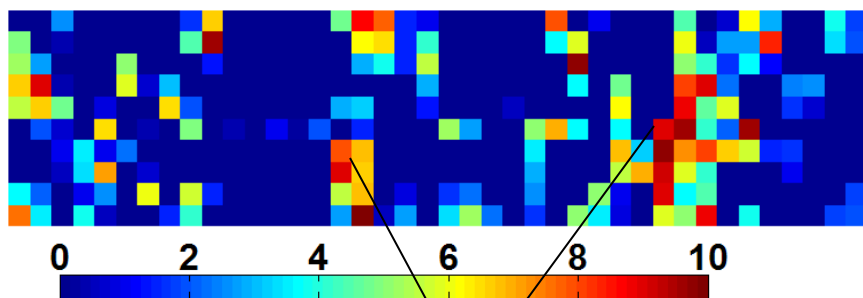


July 02, 2002

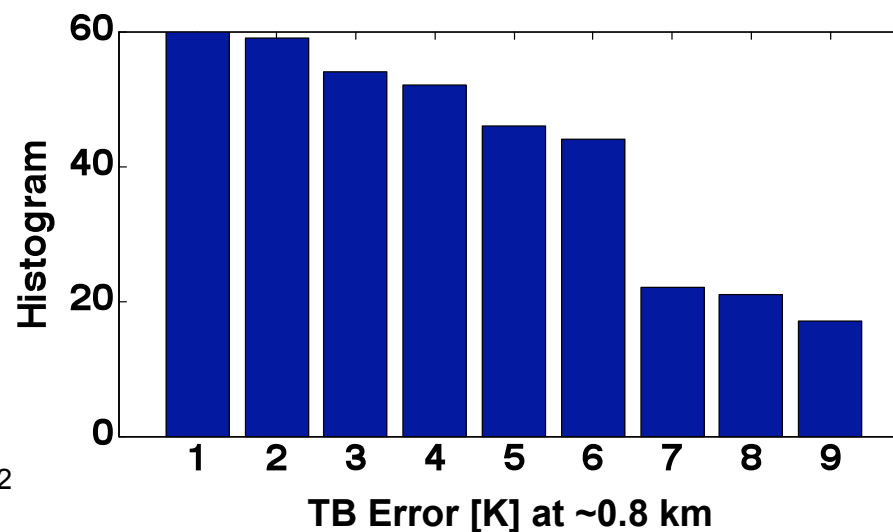
Reconstructed  $T_B$  at 0.8 km using Approach 2



Errors in reconstructed  $T_B$  at Res: 0.8 km



High errors are observed for  
pixels having trees with VWC > 5 kg/m<sup>2</sup>



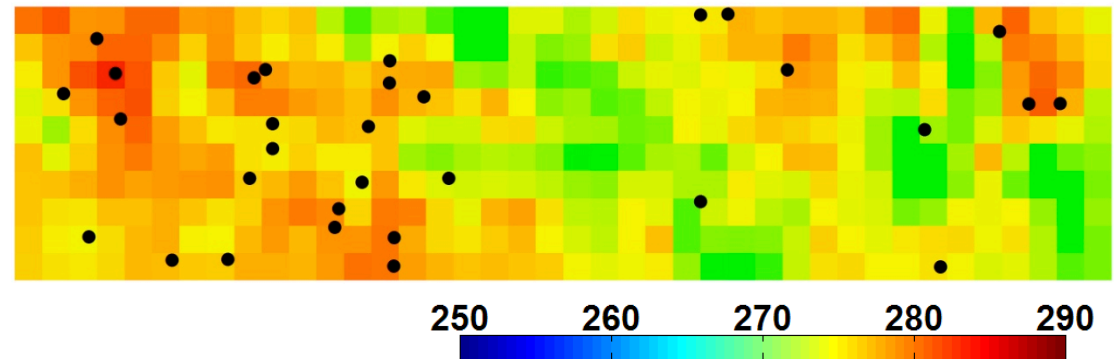


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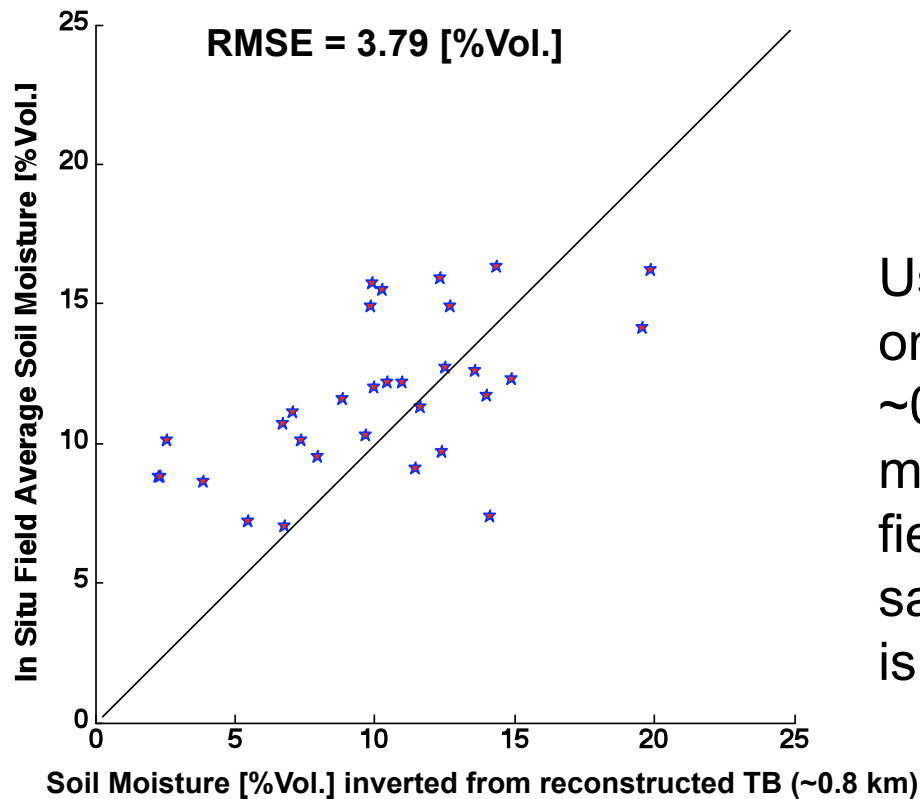
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## Soil moisture Retrieval from Reconstructed $T_B$ at 0.8 km

July 02, 2002



● Soil moisture sampling site



Using single channel algorithm (tau-omega model) disaggregated  $T_B$  (h-pol) at ~0.8 km is inverted to volumetric soil moisture and compared with the in situ field averaged soil moisture for the sampling sites. An RMSE of 3.79 [%Vol.] is obtained.



# Conclusion and Issues

## Conclusion

1. Feasibility of combined active/passive algorithm approach has been demonstrated using simulated and PALS SMEX02 dataset
2. Retrieval accuracy within 4 [%Vol.] for VWC < 5 kg/m<sup>2</sup> at 10 km spatial resolution is achievable

## Issues

1. Simulated data (OSSE) do not test every assumption/approximation in the algorithm. However, PALS data are used to verify algorithm assumptions (e.g., linear  $TB\text{-}\log[\sigma]$  relationship assumption).
2. Optimization of algorithm details is needed (e.g., time-horizon for  $\beta$ -estimation; treatment of sub-40km heterogeneity through relating  $\beta$  to ancillary data).
3. Implementation of algorithm options over larger domains (e.g., CONUS) is in progress with inclusion of appropriate errors and biases in the inputs due to satellite orbital sampling.
4. Additional time series approaches are being considered to improve algorithm

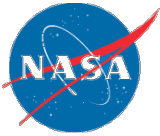




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Backup

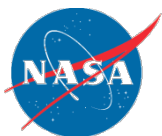


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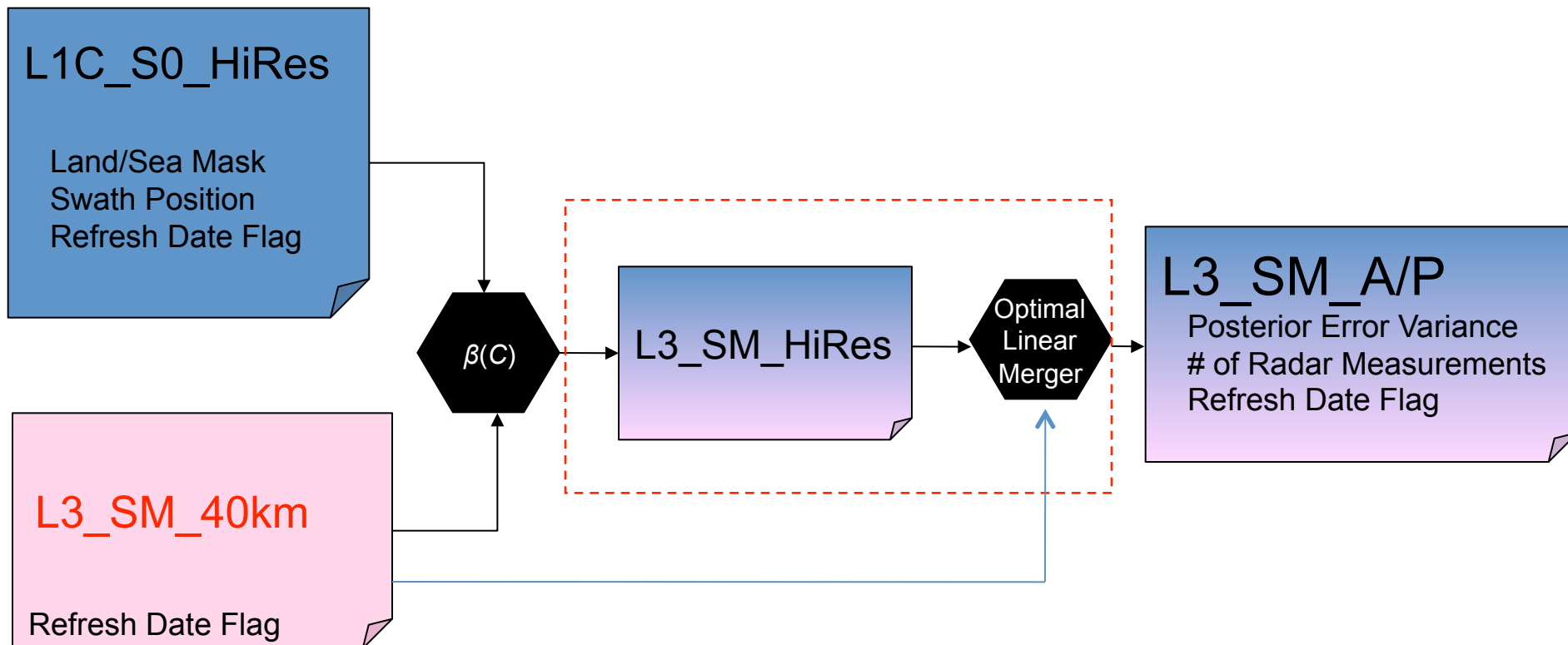
## Product Objectives

Mapping radars are capable of a very high spatial resolution but, since radar backscatter is highly influenced by surface roughness, vegetation canopy structure and water content, they have a low sensitivity to soil moisture. Various algorithms for retrieval of soil moisture from radar backscattering have been developed, but they are only valid in low-vegetation water content conditions. In contrast, the spatial resolution of radiometers is typically low, the retrieval of soil moisture from radiometers is well established and radiometers have a high sensitivity to soil moisture. To overcome the individual limitations of the passive and active approaches, the Soil Moisture Active and Passive (SMAP) mission is combining the two technologies. The accurate retrievals of soil moisture at the coarse resolution of the radiometer need to be combined with the relatively less accurate soil moisture information from the high resolution radar measurements in order to yield an intermediate scale soil moisture data product. The merging of radar and radiometer measurements and retrieved information yields the SMAP Hydrometeorology Product at intermediate (10 km) scale called L3\_SM\_A/P.



## Data Flow: L3\_SM\_A/P Time-Series Algorithm

### Approach 3



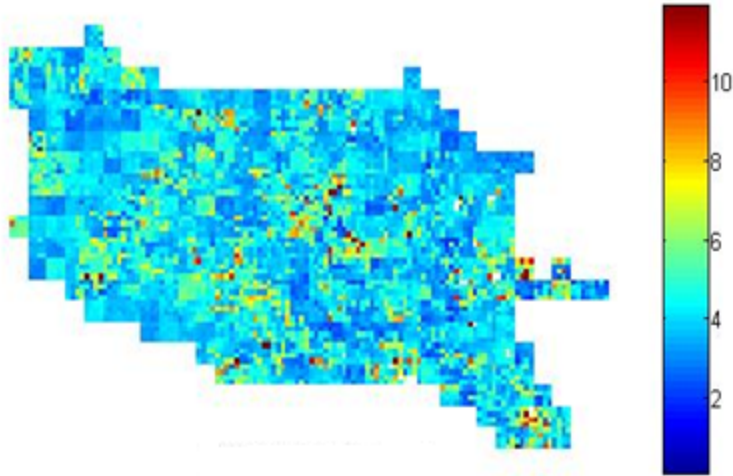
### Other Inputs:

1. Bias error statistics of input products
2. Squared error statistics of input products



## Approach using L3\_SM\_40km

Output from 4 month OSSE data



$$\theta(C, t) = \alpha(C) + \beta(C) \log_{10} \left( \frac{1}{nf} \sum_{i=1}^{nf} \sigma_{vv}(F_i, t) \right)$$

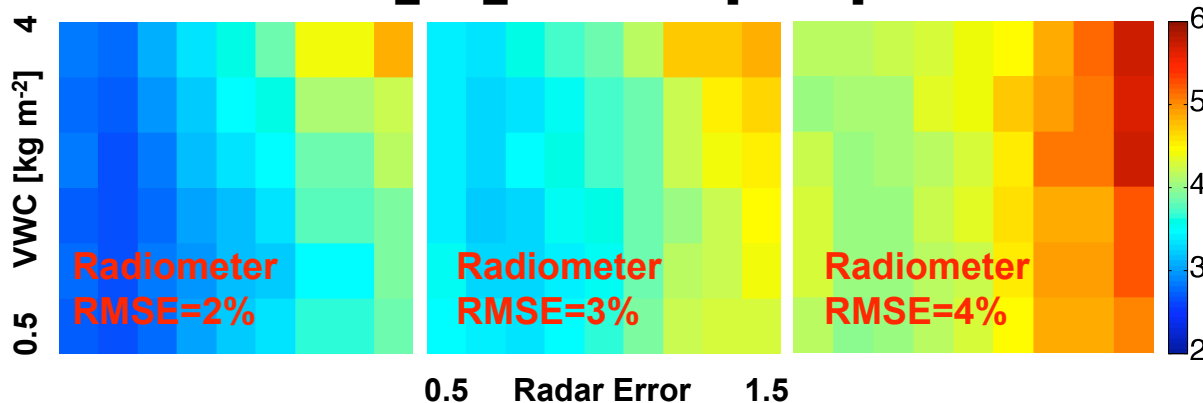
$$\Delta(\cdot)_t = (\cdot)_t - (\cdot)_{t-t_R} \quad \delta(\cdot) = (\cdot) - \langle \cdot \rangle$$

$$\theta(M_n, t) = \theta(M_n, t - t_R) + \beta(C) \Delta \log[\sigma(M_n, t)]$$

$$\theta(M_n, t) = \theta(C, t) + \beta(C) \delta \log[\sigma(M_n, t)]$$

Pixelwise RMSE at Res: ~9 km  
for input Radiometer RMSE: 4 [%Vol.]

L3\_SM\_A/P RMSE [Vol.%]



The results show that RMSE of L3\_SM\_A/P is always dependent and greater than on the input RMSE of L3\_SM\_40km